

WISE/NEOWISE OBSERVATIONS OF THE HILDA POPULATION: PRELIMINARY RESULTS

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ABSTRACT

We present the preliminary analysis of 1023 known asteroids in the Hilda region of the solar system observed by the NEOWISE component of the *Wide-field Infrared Survey Explorer* (WISE). The sizes of the Hildas observed range from ~ 3 to 200 km. We find no size–albedo dependency as reported by other projects. The albedos of our sample are low, with a weighted mean value of $p_V = 0.055 \pm 0.018$, for all sizes sampled by the NEOWISE survey. We observed a significant fraction of the objects in the two known collisional families in the Hilda population. It is found that the Hilda collisional family is brighter, with a weighted mean albedo of $p_V = 0.061 \pm 0.011$, than the general population and dominated by D-type asteroids, while the Schubart collisional family is darker, with a weighted mean albedo of $p_V = 0.039 \pm 0.013$. Using the reflected sunlight in the two shortest WISE bandpasses, we are able to derive a method for taxonomic classification of $\sim 10\%$ of the Hildas detected in the NEOWISE survey. For the Hildas with diameter larger than 30 km, there are $67^{+7}_{-15}\%$ D-type asteroids and $26^{+17}_{-5}\%$ C-/P-type asteroids (with the majority of these being P-types).

Key words: infrared: planetary systems – minor planets, asteroids: general – surveys

Online-only material: machine-readable table

1. INTRODUCTION

The Hildas are a population of asteroids in the 3:2 mean motion resonance with Jupiter, so that their orbital semimajor axes are at ~ 4.0 AU. It is believed to be populated by low-albedo C-, P- and D-type asteroids (Gradie et al. 1989). Due to the heliocentric distance of the Hildas, they are believed to have experienced less heating and are assumed to be of more pristine composition than objects in the main belt. Jones et al. (1990) found that the P- and D-types appear anhydrous and Luu et al. (1994) were unable to find any absorption bands in the infrared that were indicative of organics. More recently, however, near-infrared spectra of several D-type Jovian Trojans have been reported containing these bands (Emery & Brown 2003) and the hydration band near $3\ \mu\text{m}$ has been reported only for a few inner main-belt P- and D-types (Rivkin et al. 2002; Kanno et al. 2003). Both P- and D-types may, however, contain significant amounts of hydrosilicates without showing any detectable absorption bands if their surfaces are rich in opaque phases (Cruikshank et al. 2001). Carvano et al. (2003) pointed out that inner belt D-type objects often have concave spectral shapes and higher albedos compared to the outer belt D-types, suggesting that they may be compositionally different. Thus, at present the Hildas are assumed to be composed of a mixture of organics, anhydrous silicates, opaque material, and ice (Bell 1989; Gaffey & Wu 1989; Vilas 1994), but with only one D- and no P-type analogues among the meteorites found on Earth it is very difficult to accurately determine their compositions (Hiroi et al. 2001).

The composition of outer belt asteroids by CCD spectroscopy has been studied by Vilas & Smith (1985), Dahlgren & Lagerkvist (1995), and Dahlgren et al. (1997). These authors found that the D-type objects make up 34% of the

numbered Hilda asteroids at that epoch, with the P- and C-types making up 28% and 2%, respectively. They also found a spectral-slope–asteroid-size relation among the Hilda population, implying a size-dependent surface composition where the P-types dominate at larger sizes. They suggested that the main size-dependent physical process acting on the Hildas are their mutual collisions; thus if D-types are more fragile than the P-types, this will favor disruptive collisions among the D-type precursors. Gil-Hutton & Brunini (2008) used the Sloan Digital Sky Survey (SDSS) sample of 122 Hilda asteroids to show that this size–taxonomy correlation appears to only be valid for $H < 12$, i.e., the largest objects.

Thermal observations of 23 Hildas were collected by the *Infrared Astronomical Satellite* (IRAS; Matson et al. 1986; Tedesco et al. 1992; Ryan & Woodward 2010). Ryan & Woodward (2011) reported thermal observations of an additional 64 objects in the Hilda population collected with the *Spitzer Space Telescope*. They reported an apparent size and albedo dependency, with lower sizes yielding higher albedos.

The population of minor planets in the first-order mean motion resonances with Jupiter, i.e., the Jovian Trojan, Hilda, and Thule populations, are possible footprints of the orbital evolution of the giant planets. Stability or instability of these populations is directly related to the orbital configuration of the giant planets, and they also provide constraints and clues to the nature and amount of migration by Jupiter and other details of its dynamical behavior (Brož & Vokrouhlický 2008). The current configuration of the giant planets is the result of some dynamical evolution in the early solar system and recently the so-called Nice model has gained significant traction in describing this evolution (Gomes et al. 2005; Morbidelli et al. 2005; Tsiganis et al. 2005). This model puts Jupiter and Saturn interior to their mutual 1:2 mean motion resonance (Morbidelli et al. 2007) with

the event of crossing this resonance having major influence on not only the final configuration of the planets, but also strongly affecting the distribution of minor planets. Studies by Morbidelli et al. (2005) and Brož & Vokrouhlický (2008) show that such a scenario would destabilize the Jovian Trojan and Hilda populations, then repopulating them later during the same phase of the dynamical evolution. Determination of the physical properties of the Hilda population (such as their numbers, sizes, albedos, and orbital distribution) is thus important as it allows us to compare them to that of the main-belt asteroids and Jovian Trojan populations. This could reveal clues as to whether the population is of primordial origin or was inserted into the resonance during the later stages of planet migration. In particular, the difference or similarities between the Hilda and Jovian Trojans populations puts constraints on the origin of the bodies needed to repopulate the two resonances after the migration of Jupiter.

In this paper, we will try to answer the following questions. (1) What is the albedo distribution of the Hildas and is there a size–albedo relation as reported by Ryan & Woodward (2011)? (2) What is the size–frequency distribution? (3) What is the relative fraction of C-, P- and D-type asteroids in the Hilda population? In this paper, we discuss the observations in Section 2 and select our Hilda sample in Section 3. The thermal model is described in Section 4 and the results are discussed in Section 5.

2. OBSERVATIONS

The *Wide-field Infrared Survey Explorer* (WISE) is a National Aeronautics and Space Administration (NASA) medium-class Explorer mission designed to survey the entire sky in four infrared wavelengths: 3.4, 4.6, 12, and 22 μm (denoted as W1, W2, W3, and W4 respectively; Wright et al. 2010; Mainzer et al. 2005). The survey collected over two million observations of more than 157,000 asteroids, including near-Earth objects, main-belt asteroids, comets, Hildas, Jovian Trojans, Centaurs, and scattered disk objects (Mainzer et al. 2011a). With this sample, WISE has collected infrared measurements of nearly two orders of magnitude more asteroids than its predecessor, IRAS (Matson et al. 1986; Tedesco et al. 1992, 2002). The survey started on 2010 January 14 and exhausted its secondary tank cryogen on 2010 August 5. Exhaustion of the primary tank cryogen occurred on 2010 October 1, but the survey was continued until 2011 February 1, as the NEOWISE Post-Cryogenic Mission, using only bands W1 and W2.

The WISE observations of the Hildas were retrieved by querying the Minor Planet Center (MPC) observational files for all instances of individual WISE detections of the desired objects that were reported using the WISE Moving Object Processing System (WMOPS; Mainzer et al. 2011a). The WISE survey cadence resulted in most minor planets receiving on average 10–12 observations over ~ 36 hr (Wright et al. 2010; Mainzer et al. 2011a). The resulting set of position/time pairs were used as the basis for a query of WISE source detections in individual exposures (known as Level 1b images) using the Infrared Science Archive (IRSA). To ensure that only observations of the moving objects were returned from the query, a search radius of $0''.3$ from the observations in the MPC observation file was used. Since WISE collected a single exposure every 11 s, the modified Julian date was also required to be within 4 s of the time specified by the MPC. Only observations with 0 and p in the artifact identification CC_FLAG were used, where 0 indicates that no evidence of

known artifacts were found at the position and p indicates that an artifact may be present. We have found that observations with CC_FLAGS of p are generally non-distinguishable from the non-flagged observations, indicating that the First-Pass version of the WISE data processing pipeline is very conservative in its artifact identification. Adding the observations flagged with p recovers about 20% more observations. Some of the Hildas have W3 magnitudes brighter than 4, at which point the detector approached experimentally derived saturation limits. A linear correction was performed to account for the inaccuracy in the point-spread function of these slightly saturated sources and the W3 magnitude error was set to 0.2 mag.

In order to avoid having low-level noise detections and/or cosmic rays contaminating our thermal model fits, we require that each object should have at least three uncontaminated observations in a band. Any band that did not have at least 40% of the observations of the band with the most numerous detections (in general W3 or W4 for the Hildas) was discarded even if it has three or more detections. WMOPS was designed to reject inertially fixed objects such as stars and galaxies in bands W3 and W4, but with stars having approximately 100 times higher density in bands W1 and W2, it is more likely that asteroid detections in these bands are confused with inertial sources. We remove such confused asteroid detections by cross-correlating the asteroid detections with sources in the WISE atlas and daily co-added catalogs from IRSA. Objects within $6''.5$ (equivalent to the WISE beam size at bands W1, W2, and W3) of the asteroid position appearing in the co-added sources at twice and in more than 30% of the total number of coverages of a given area of sky were considered to be inertially fixed sources contaminating the asteroid photometry, and these observations were removed from the thermal fitting.

3. OBJECT SELECTION

In this paper, we will only consider the objects that have well-determined orbits that securely define them as Hildas. The Hildas are in the 3:2 mean motion resonance with Jupiter, which lies at $a \sim 3.9$ (see Figure 1). We define the Hildas in the most general sense, allowing their semimajor axis to be in the range 3.7–4.2 AU, with an eccentricity less than 0.4 and an inclination less than 30° . To make sure that the orbits are generally secure we also require the observed arc length to be at least 18 days, which is longer than that needed for orbital determination to be able to differentiate between main-belt asteroids, Hildas, and Jovian Trojans. There are 1028 objects in the data set of objects observed by NEOWISE during the fully cryogenic part of the survey that satisfy these criteria (see Figure 2), and we label this sample as the long-arc Hildas (LAH). Of these, 923 objects were associated with previously known objects, while 105 objects were new discoveries that have subsequently been linked to incidental astronomy in the MPC one-night database or have received optical follow-up after the object was reported to the MPC.

We note that using these slightly relaxed criteria means that a handful of objects that are in Hilda-like orbits, which may not actually be in the 3:2 mean motion resonance, have been included in the LAH sample. Accurate long-term orbital integration of the Hildas to weed out these handful of objects, making up at most 1%–2% of the full sample, is beyond the scope of this paper, and the low number of objects in question are too few to significantly influence the results presented.

There is a significant overlap in the observed WISE magnitudes between the Hildas and Main Belt Asteroids (MBAs; see

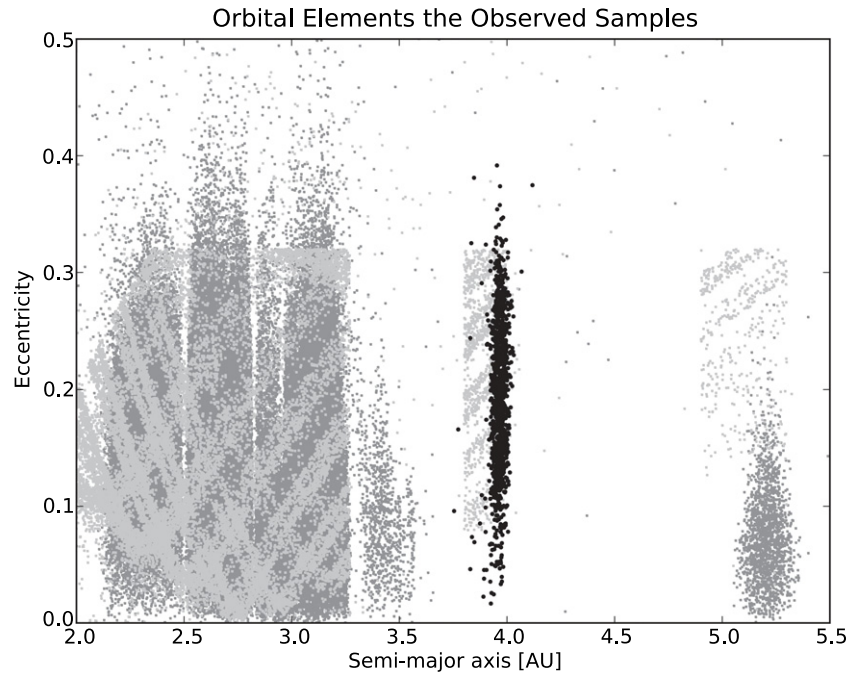


Figure 1. Semimajor axes and eccentricities of the objects detected by NEOWISE. The black shows the Hilda objects with well-established orbits that constitute the long-arc Hilda (LAH) sample. The dark gray gives the objects with observational arc lengths greater than 18 days, indicating that they were either already known at the time of *WISE* observation or subsequently had optical follow-up. The light gray indicates objects with observational arc lengths less than 18 days and are generally *WISE* discoveries with no optical follow-up. The pattern seen in these short arc objects is an artifact of the procedures used by the MPC in deriving preliminary orbits for objects with such short arcs and is not a real property of the objects' orbits.

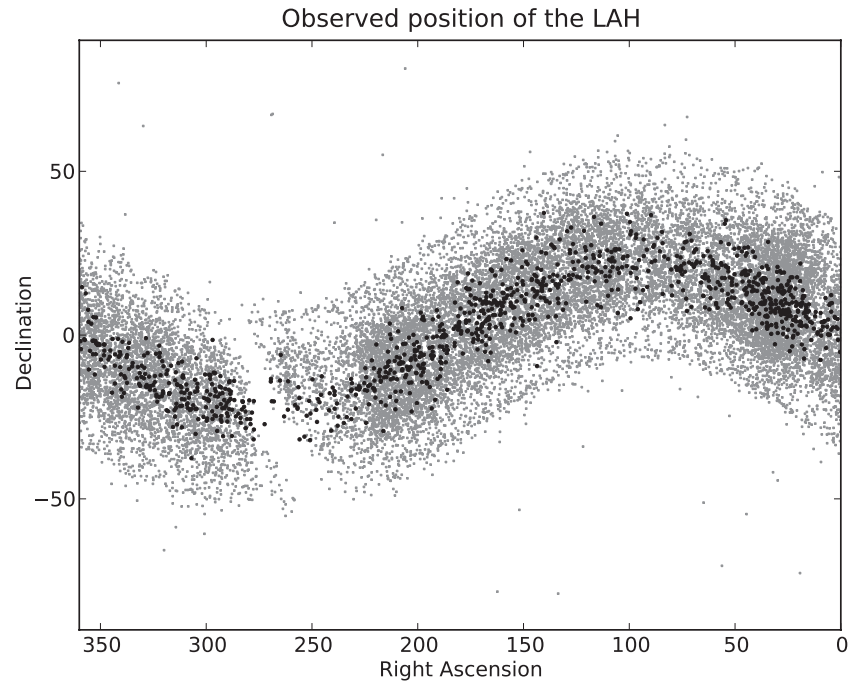


Figure 2. Observed sky-plane position of the LAH (in black) compared to the short arc length sample (in gray).

Figure 3). While in Grav et al. (2011b) we were able to define a sample of candidate Jovian Trojans, the significant color overlap with the MBAs makes this unobtainable for the Hildas. Thus in this paper, we do not attempt to disentangle the objects in these populations with short observational arcs (less than 18 days). It is expected that current large sky surveys like the Catalina Sky Survey, Lincoln Near-Earth Asteroid Research (Stokes et al. 2000), and the Panoramic Survey Telescope and Rapid Response System (Pan-STARRS; Wainscoat et al. 2010)

will provide optical follow-up of a significant fraction of these objects in the next few years. At that point, we will update the preliminary results presented in this work.

4. PRELIMINARY THERMAL MODELING

Preliminary thermal models for each of the Hildas detected by WMOPS during the cryogenic portion of the survey and using the First-Pass Data Processing Pipeline (version 3.5; Cutri et al.

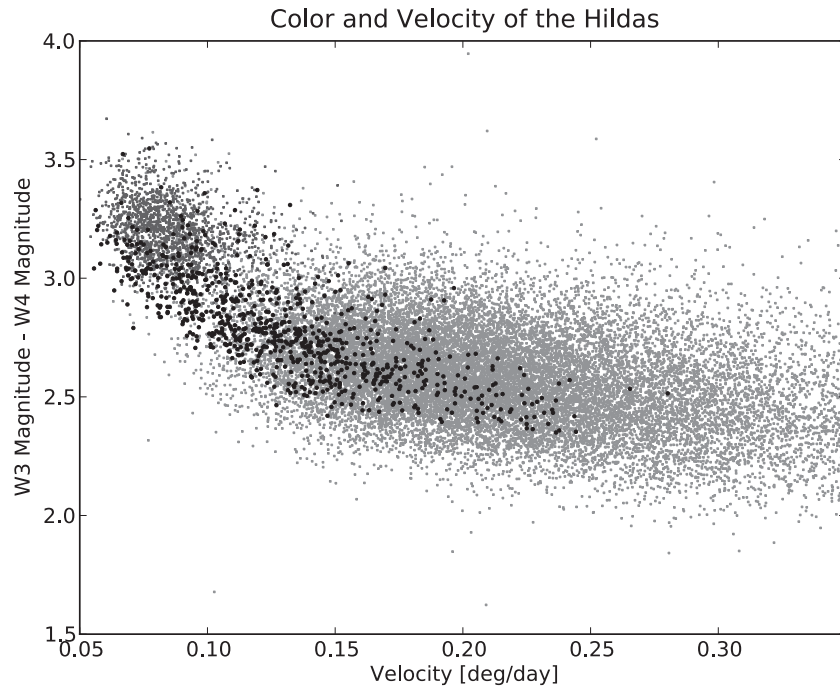


Figure 3. Thermal color and observed sky-plane velocity of the LAH (in black) compared to the short observational arc sample (in gray).

2011) described above have been computed (these models will be recomputed when the final data processing is completed sometime during the fall of 2011). As described in Mainzer et al. (2011d), the spherical near-Earth asteroid thermal model (NEATM; Harris 1998) was used. The NEATM introduced the so-called beaming parameter η to account for cases intermediate between zero thermal inertia (the standard thermal model or STM; Lebofsky et al. 1978) and infinite thermal inertia (the fast rotating model or FRM; Veeder et al. 1989; Lebofsky & Spencer 1989). In the STM, η is set to 0.756 to match the occultation diameters of Ceres and Pallas, while in the FRM, η is equal to π . In the NEATM, η is a free parameter that can be fitted if two or more thermal bands are available, or using a single thermal band if a priori information of diameter and albedo is available from spacecraft or occultation observations.

For each object, a spherical surface was approximated using a set of triangular facets (cf. Kaasalainen 2004). While some Hildas are non-spherical, the *WISE* observations generally consist of 8–10 observations uniformly distributed over ~ 36 hr for each object, so any rotational variation is generally averaged out and the model yielding the effective diameter, D_{eff} . Caution needs to be exercised when interpreting the meaning of an effective diameter in cases where objects have high-rotational amplitudes. However, all objects in our sample have peak-to-peak amplitudes less than ~ 0.5 mag, and less than 10% have peak-to-peak amplitudes greater than ~ 0.3 mag. We therefore feel confident that assuming spherical shapes for our models does not significantly affect the results derived in this paper.

Thermal fluxes were computed for each individual *WISE* measurement using the thermal model, ensuring that the correct Sun–observer–object geometry was used. The temperature of each facet was computed for the thermal distribution assumed by the NEATM model, and color corrections were applied to each facet based on Mainzer et al. (2011d). In addition, adjustments of the W3 effective wavelength blueward by 4% from $11.5608 \mu\text{m}$ to $11.0984 \mu\text{m}$, and of the W4 effective wavelength redward by 2.5% from $22.0883 \mu\text{m}$ to $22.6405 \mu\text{m}$ were used. Due to the

red–blue calibrator discrepancy reported in Wright et al. (2010) and Mainzer et al. (2011d) offsets to the W3 and W4 magnitude zero points of -8% and $+4\%$, respectively, were applied. In general, orbital elements and absolute magnitudes were taken from the MPC catalogs, and we assumed an error of 0.3 mag for the absolute magnitude, H . emissivity, ϵ , was assumed to be 0.9 for all wavelengths (cf. Harris et al. 2009), and the slope parameter, G , in the magnitude–phase relationship was set to 0.15 unless an improved value exists in the MPC catalogs.

For Hildas with measurements in both W3 and W4, the beaming parameter η was determined using a least-square minimization, but was constrained to be less than the upper bound set by the FRM case, π . The resulting distribution based on 747 Hildas with long observational arcs is shown in Figure 4 and has a weighted average of $\eta = 0.85 \pm 0.12$. To understand how the errors on the derived beaming influence this distribution, we employed a Monte Carlo (MC) approach. We varied the beaming for each object randomly using a Gaussian error distribution with FWHM of the associated derived error. After each of the 793 objects’ beaming values were varied in this fashion, the distribution for each new set was computed. Using 100 such varied sets we computed the mean and associated standard deviation for each bin. The resulting distribution is shown in Figure 4 as the points with associated error bars. The double Gaussian curve that best fits this distribution has a mean of 0.82 ± 0.08 and 1.02 ± 0.19 , with the lower mean Gaussian having a peak of ~ 5 times higher than the higher mean Gaussian. For the objects in the LAH with only one thermal measurement, the beaming values cannot be fitted and instead are given a value 0.85 ± 0.12 . The beaming distribution is similar to that of the Jovian Trojans (Grav et al. 2011b) and is slightly lower than the value of $\eta = 0.91$ derived based on 23 objects detected in two or more bands in the *IRAS* survey (Ryan & Woodward 2010, 2011).

For the Hildas bands W1 and W2 are generally dominated by reflected light. The flux due to reflected sunlight was computed for each *WISE* band as described in Mainzer et al. (2011d) using

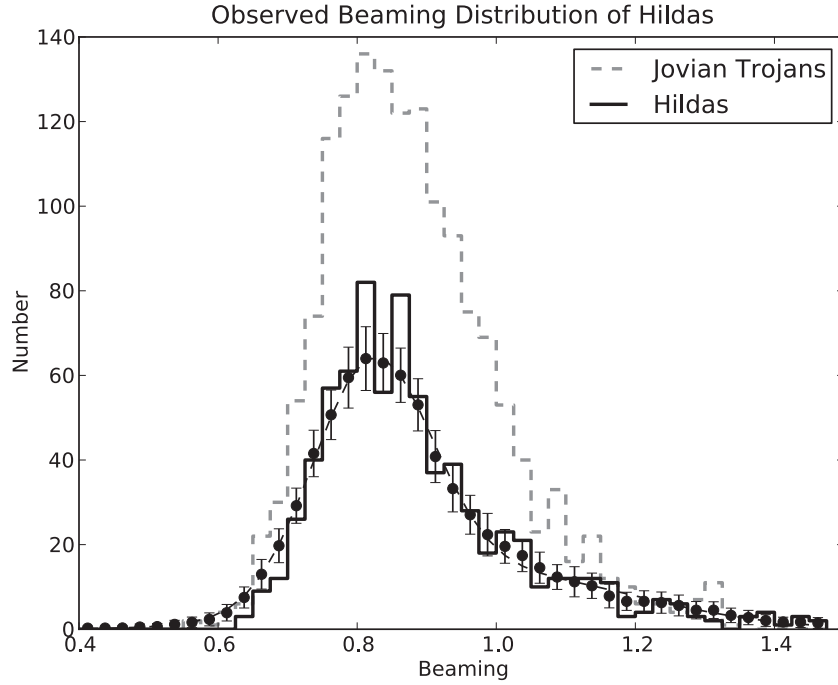


Figure 4. Distribution of the beaming value, η , based on the 747 objects for which there were observations in both the W3 and W4 bands.

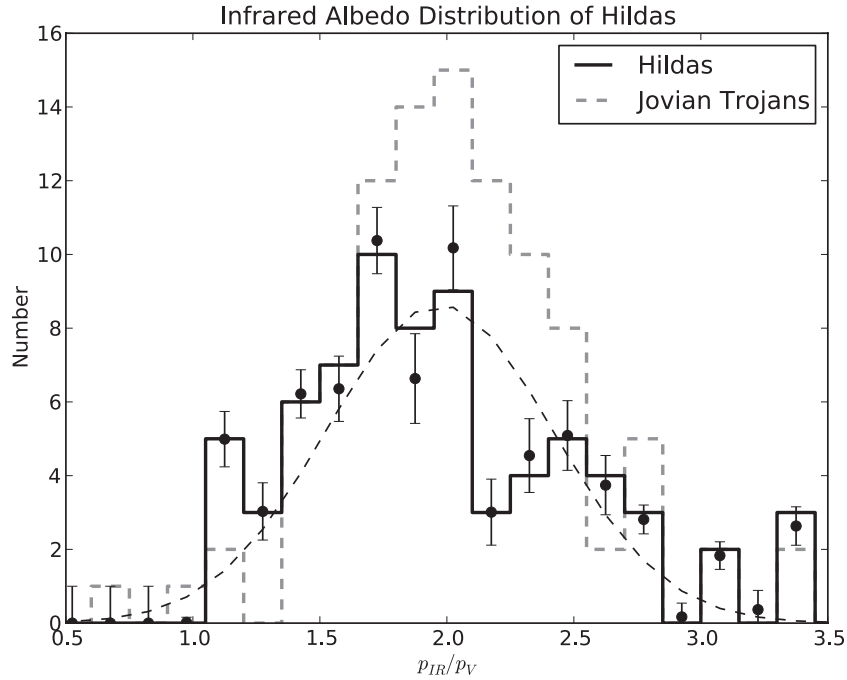


Figure 5. Distribution of the p_{IR}/p_V values based on the 72 objects for which there were observations in either the W1, W2, or both bands. The points with associated error bars is the Monte Carlo (MC) error analysis described in the text based on 100 trial runs. The best-fit single Gaussian distribution, which has a mean and standard deviation of 1.9 ± 0.4 , is shown as a dashed line.

the International Astronomical Union phase curve correction (Bowell et al. 1989). The facets that were illuminated by reflected sunlight and observable by *WISE* were corrected using color corrections appropriate for a G2 V star (Wright et al. 2010). In order to compute the fraction of total luminosity due to reflected light, the relative reflectance at bands W1 and W2, dubbed p_{IR}/p_V , was introduced. The distribution for p_{IR}/p_V for the 72 Hildas with long observational arc that had detections in either W1, W2, or both is shown in Figure 5. The weighted average for the distribution is 1.9 ± 0.5 , which is slightly lower

than that found for the Jovian Trojans (Grav et al. 2011b). For objects where there are no W1 and W2 observations, p_V/p_{IR} is assumed to be 1.9 ± 0.5 .

5. RESULTS

We were able to derive diameters and albedos for 1023 of the Hildas in the LAH sample. The results are plotted in Figure 6, together with the 23 objects observed by *IRAS* (Ryan & Woodward 2010) and 64 objects observed by *Spitzer* (Ryan

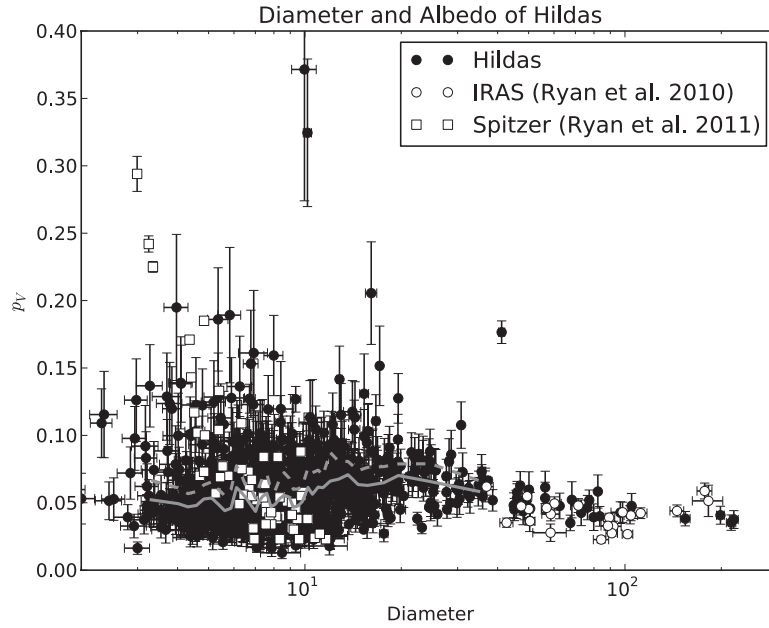


Figure 6. Diameters and albedos of the 1023 Hildas with long observational arc for which a thermal model was derived are shown. The values for the 23 Hildas observed by *IRAS* (Ryan & Woodward 2010) and 64 objects observed by *Spitzer* (Ryan & Woodward 2011) are also plotted. The calculation of the running median and the absolute median deviation is shown in gray.

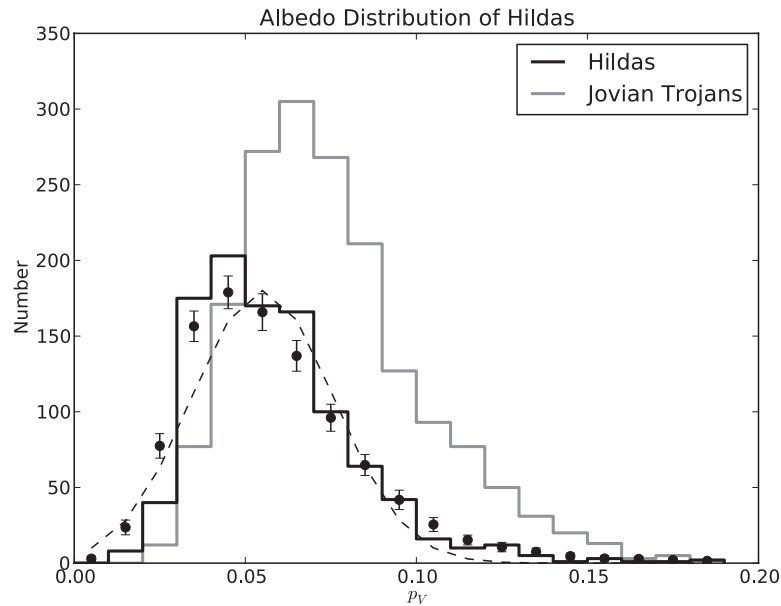


Figure 7. Albedo distribution of the 1023 Hildas for which a thermal model was derived is shown. The distribution using the MC error analysis as described in Section 4 is shown as black points with associated error bars. A best-fit single Gaussian distribution with mean and standard deviation of 0.055 ± 0.021 is shown as a dashed line.

& Woodward 2011). The albedo distribution is homogeneous and very low with a weighted mean of 0.055 ± 0.018 (see Figure 7). There is only a handful of objects with higher albedo, $p_V > 0.15$, that would be indicative of high-albedo interlopers into a generally dark population. The albedo distribution is clearly darker than the Jovian Trojan population (Grav et al. 2011b). We caution that although there does appear to be a broadening of the albedo distribution for smaller sizes, this does not mean that there is a correlation between size and albedo as reported by other authors (Ryan & Woodward 2011). We computed the running median and running median absolute deviation across the size range observed using a variety of window sizes and found that both the median and deviation

remain consistent with the weighted mean across the full size range. The maximum median of 0.065 ± 0.008 is found around 20 km and then decreases slightly to 0.047 ± 0.010 at 4 km. The broadening seen at smaller sizes is thus a natural increase in the number of outlier measurements following Gaussian errors due to the increase of the total number of objects at smaller sizes, not a broadening due to some physical difference or process happening on the surface.

Figure 8 shows the albedo and diameter from the *IRAS* and *Spitzer* samples compared to that from our sample. It is seen that the *IRAS* diameters derived by Ryan & Woodward (2010) are systematically slightly larger than our values, a result that was also seen in comparison of the diameters of

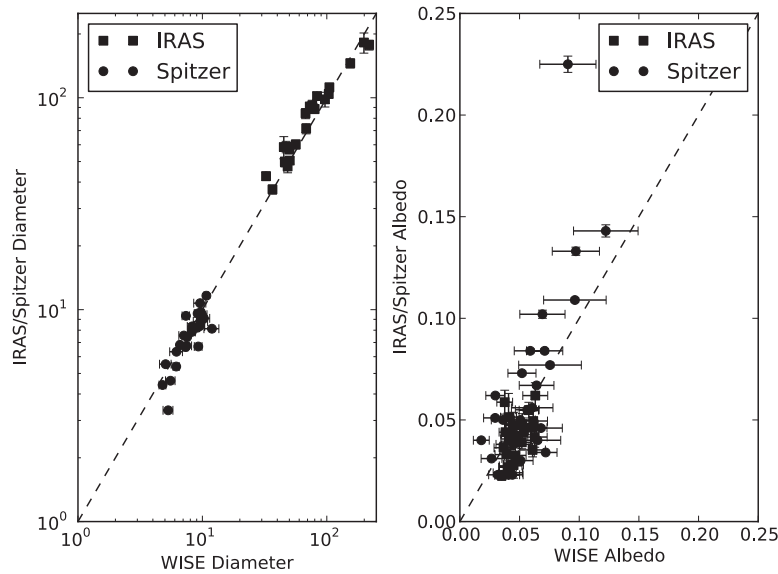


Figure 8. Comparison of the derived diameters (left panel) and albedo (right panel) from this paper and those from Ryan & Woodward (2010, 2011).

Table 1
Thermal Model Fits

Object	H	G	D	p_V	η	p_{IR}	# obs
M2587	14.40	0.15	7.21 ± 0.41	0.059 ± 0.014	0.846 ± 0.073	0.112 ± 0.026	0 0 13 13
F4603	13.80	0.15	10.74 ± 0.50	0.046 ± 0.009	0.863 ± 0.059	0.088 ± 0.016	0 0 10 10
O7879	14.80	0.15	6.64 ± 0.54	0.048 ± 0.011	1.076 ± 0.126	0.091 ± 0.022	0 0 10 9
52068	12.70	0.15	15.57 ± 0.25	0.061 ± 0.013	0.822 ± 0.022	0.115 ± 0.025	0 0 12 12
O5093	14.60	0.15	8.23 ± 0.52	0.038 ± 0.006	1.057 ± 0.103	0.072 ± 0.011	0 0 15 15
J4501	15.10	0.15	4.95 ± 0.28	0.066 ± 0.015	0.767 ± 0.074	0.125 ± 0.028	0 0 15 14
10296	12.70	0.15	14.11 ± 0.49	0.074 ± 0.015	0.791 ± 0.045	0.140 ± 0.029	0 0 13 13
B9922	14.30	0.15	11.57 ± 0.71	0.025 ± 0.006	1.012 ± 0.089	0.048 ± 0.011	0 0 11 10
C0618	13.90	0.15	9.72 ± 0.24	0.051 ± 0.010	0.792 ± 0.036	0.098 ± 0.018	0 0 12 12
11542	11.30	0.15	29.69 ± 0.19	0.061 ± 0.013	0.866 ± 0.011	0.108 ± 0.013	10 11 12 12

(This table is available in its entirety in machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)

the other populations (Mainzer et al. 2011c). The diameters and albedos derived by Ryan & Woodward (2011) from their *Spitzer* survey are generally in very good agreement with the values derived here, although there are small systematic shifts with the objects being slightly smaller and darker in their results. NEOWISE observed one of the five high-albedo objects, (128295) 2003 WD111, used by Ryan & Woodward (2011) to argue for the size–albedo dependency. This object only has an albedo of $p_V = 0.09 \pm 0.02$ in our data, less than half the value reported in that paper. It should be noted here that the uncertainties quoted in Table 2 of Ryan & Woodward (2011; plotted in Figure 8) are understated as *Spitzer* 24 μ m MIPS photometric observations that have a minimum calibration uncertainty of 4% according to the *Spitzer* Instrument Handbook (<http://irsa.ipac.caltech.edu/data/SPITZER/docs/mips/>). While back-of-the-envelope error calculations from uncertainties in H (using ± 0.1 mag uncertainty, rather than the more realistic ± 0.3 mag uncertainty used in this paper) and the beaming η are presented in their paper, these uncertainties were not folded into the table of derived values they presented. This makes it difficult to accurately determine why and if the derived values in this paper and that of Ryan & Woodward (2011) are significantly different. The *WISE* results have been extensively calibrated against asteroids with known diameter in Mainzer et al. (2011d) and a comparison with the *IRAS* sample is found in Mainzer

et al. (2011c). The latter paper shows that the *IRAS*-based diameter values derived by Ryan & Woodward (2010) appear to be systematically larger than diameters from radar, occultation, or spacecraft flybys. This systematic offset is not seen nearly as strongly in the original *IRAS* catalog by Tedesco et al. (2002). The validity of the claim of an albedo dependency with diameter put forth in Ryan & Woodward (2011) will be studied in detail in Section 5.5 below.

The diameter and beaming values for the 747 Hildas with long observational arcs that had observations in two thermal bands are shown in Figure 9. The beaming is generally centered around the weighted mean of 0.85 ± 0.12 , although there is a small increase of higher beaming values at smaller sizes. This is most likely a result of the increasing number of objects at smaller sizes, resulting in more outlier objects in the wings of the beaming distribution, rather than a real physical widening of beaming values for the population. An electronic table with the thermal fit results is available in the online journal and Table 1 shows an example of the form and content included for each object.

5.1. Dual Epoch Objects

There are 66 objects in our sample that NEOWISE observed at two different epochs during the cryogenic survey. For each of these objects, each epoch was fitted independently. The results

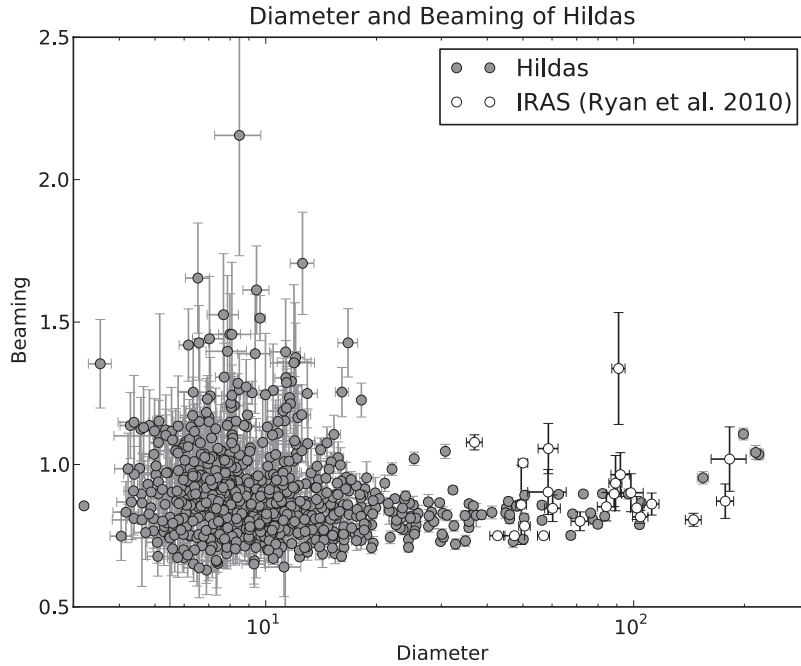


Figure 9. Shown are the diameters and beaming values of the 747 Hildas with long observational arcs for which a thermal model with varied beaming value was derived. The values for the 23 Hildas observed by *IRAS* (Ryan & Woodward 2010) are also shown for comparison.

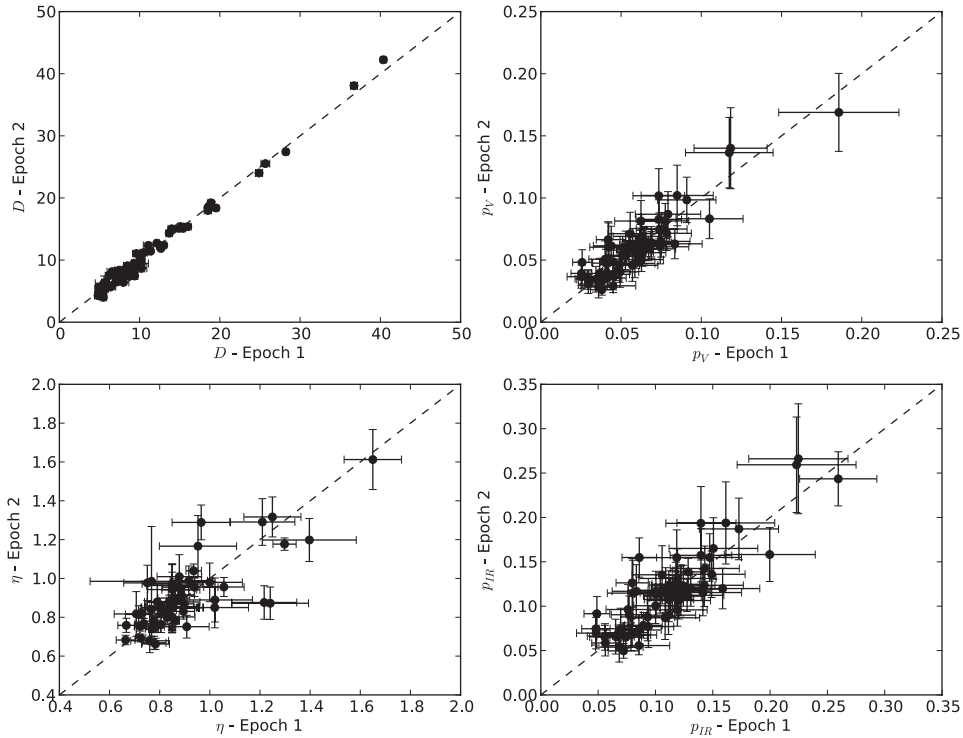


Figure 10. Comparison of the thermal model variables for the 66 objects for which *WISE* observed at two different epoch during the cryogenic survey.

are shown in Figure 10, and it is seen that for all derived parameters the difference between the values in the two epochs are consistent to within the derived errors.

5.2. High-albedo Objects

There are eight objects with $p_V > 0.17$ that could be higher albedo interlopers into a generally dark Hilda population (see Table 2). Of the eight only one, (3290) Azabu, has SDSS photometry (Gil-Hutton & Brunini 2008) and none have any

spectral observations. Gil-Hutton & Brunini (2008) identified (3290) Azabu as an X-complex asteroid, and the high albedo found here, $p_V = 0.32 \pm 0.08$, would make it an E-type asteroid.

5.3. Taxonomy

Several authors have classified a number of the Hildas in the Tholen taxonomy scheme, based either on multi-color photometric (Gil-Hutton & Brunini 2008) or visible wavelength spectroscopic observations (Bus & Binzel 2002; Dahlgren & Lagerkvist 1995; Dahlgren et al. 1997; Lazzaro et al. 2004;

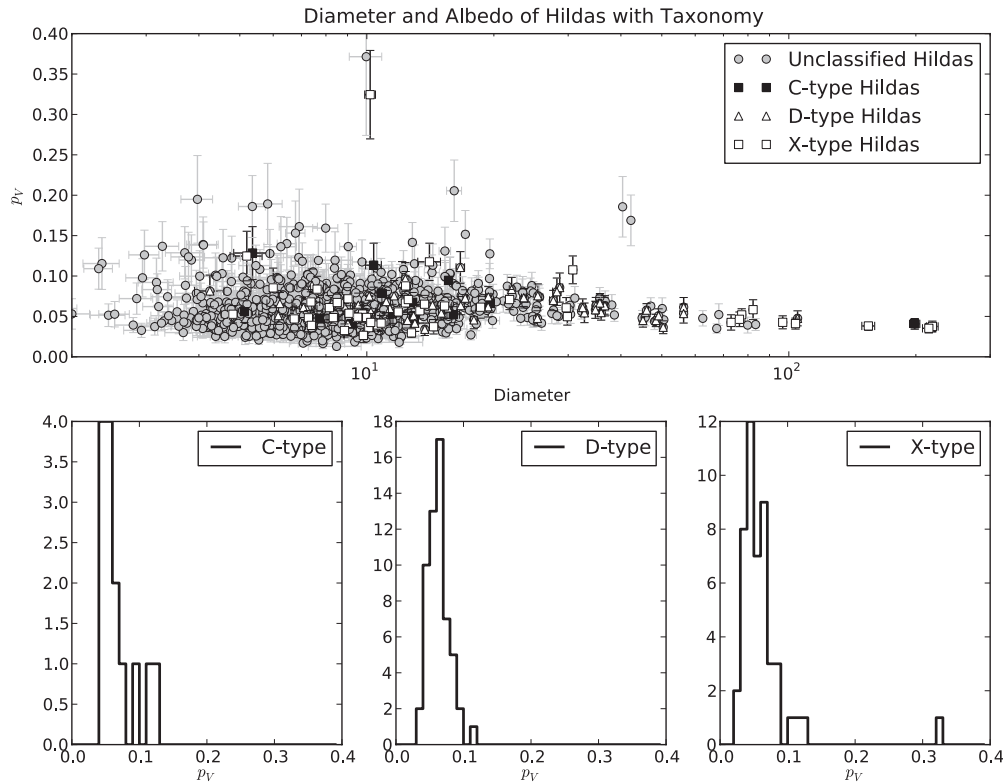


Figure 11. Shown here is the diameter and p_V of the Hildas with both unclassified and classified taxonomy from other authors (Dahlgren & Lagerkvist 1995; Dahlgren et al. 1997; Bus & Binzel 2002; Xu et al. 1995; Lazzaro et al. 2004; Gil-Hutton & Brunini 2008).

Table 2
High-albedo Hildas

Object	Diameter (km)	Beaming	Albedo
1162	41.3 ± 0.9	0.83 ± 0.03	0.18 ± 0.03
3290	10.2 ± 0.4	0.70 ± 0.06	0.32 ± 0.08
11249	10.0 ± 0.9	0.86 ± 0.14	0.37 ± 0.10
14699	16.1 ± 0.7	1.25 ± 0.09	0.21 ± 0.04
77734	5.4 ± 0.4		0.19 ± 0.04
89928	5.8 ± 0.5	0.77 ± 0.11	0.19 ± 0.05
96086	6.3 ± 0.5		0.19 ± 0.05
225800	4.0 ± 0.3		0.19 ± 0.05

Xu et al. 1995; Fornasier et al. 2011). We found 123 objects among our sample that have taxonomic classes assigned by these authors and these are plotted in Figure 11.

As mentioned in Section 4, the survey yielded 71 objects with observations in either $W1$, $W2$, or both, making it possible to derive the relative reflectance in the $W1/W2$ bands. Figure 12 shows the albedo, p_V , versus this relative reflectance for these 71 objects. The spectral class for the 36 objects in this sample that has been studied among the photometric or spectral surveys mentioned above is also given. It is seen that the C- and X-type objects cluster in the group having both low p_V and p_{IR}/p_V , while the objects classified as D-type are all in the group with low p_V and moderate p_{IR}/p_V . The low albedos of the X-complex objects indicate that these are P-types, rather than the moderate albedo M-types or high-albedo E-types. The larger range of albedos seen here in the D-type group ($p_V \sim 0.03$ – 0.10) compared to the C- and P-type groups ($p_V \sim 0.03$ – 0.06) is consistent with the albedo distribution of these types as seen in the MBAs (Mainzer et al. 2011c). We note that there is no appar-

ent way with our data alone to distinguish between the C- and P-type objects in the Hilda population.

From Figures 6 and 12 it is seen that the large objects are all C- or P-type asteroids, with the largest D-type object, (1269) Rollandia, being $D \sim 104 \pm 1$ km. This confirms the result of other surveys (Dahlgren et al. 1997). As we will see later in Section 5.5, it is clear that the known sample is more than 90% complete for sizes of 10 km or larger. Looking at our sample, there is only one object with diameter larger than 30 km for which the p_{IR}/p_V was not derived, and there are 49 objects in our sample of this size or larger. Of these, 13 land in the C- or P-type grouping in Figure 12, while 33 fall into the D-type grouping (see Table 3 for a list of objects with new taxonomic classification). Two of the objects are consistent with M-type classification. The faintest of the objects with diameter larger than 30 km is (5928) with $H = 11.4$. There are 16 objects with $H \leq 11.4$ that are not in the LAH sample and two of these have taxonomy determined by other sources (one X-type and one D-type). This means that for objects with diameter larger than 30 km the fraction of C-/P-types is $26^{+7}_{-5}\%$, while the D-type fraction is $67^{+17}_{-15}\%$. The fraction of C-/P-types are of course dominated by P-types, with (334) Chicago being the only well-defined C-type object among the Hildas and (1439) Vogtia having a possible F-type classification.

Two of the objects such as X-type ((3843) OISCA and (11542) 1992 SU21) are located among D-types. One of these, (11542) 1992 SU21 is classified based on SDSS photometry by Gil-Hutton & Brunini (2008), while the other, (3843) OISCA, was generically given E, M, or P as the possible Tholen classification by Dahlgren et al. (1997). The albedo of (3843) OISCA is $p_V = 0.11 \pm 0.01$, which would make this object an M-type asteroid. This classification leads us to believe that the objects in Figure 12 with $p_V > 0.1$ may all be M-type

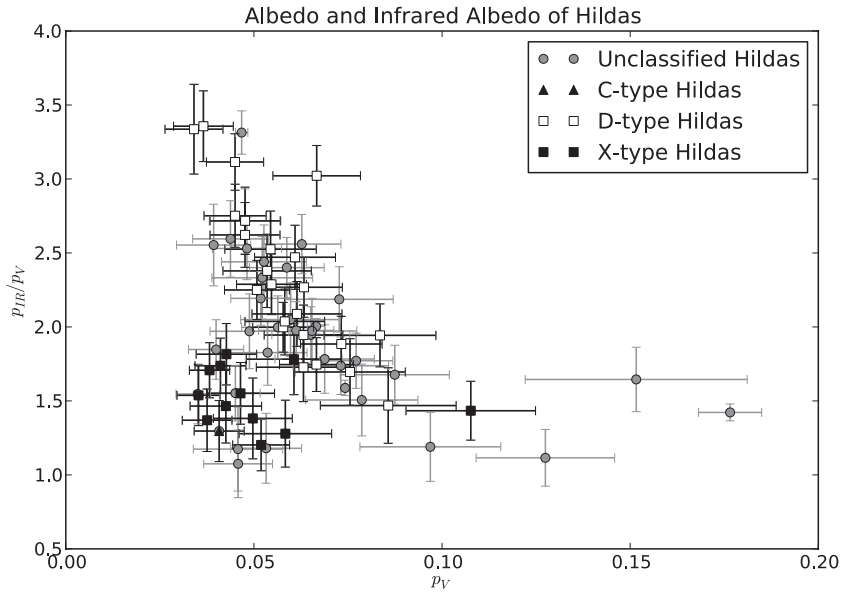


Figure 12. Visible albedo, p_V , and relative reflectance in the $W1/W2$ bands, p_{IR}/p_V , are shown. Also shown are the taxonomic classifications based on data from literature (Dahlgren & Lagerkvist 1995; Dahlgren et al. 1997; Bus & Binzel 2002; Xu et al. 1995; Lazzaro et al. 2004; Gil-Hutton & Brunini 2008; Fornasier et al. 2011).

Table 3

New or Reclassified Taxonomy of the Objects in the Hilda Population Based on the Visible Albedo and Relative Reflectance in Bands $W1/W2$

Object	Taxonomy		Albedo	p_{IR}/p_V
	Old	New		
1162		M	0.18 ± 0.04	1.42 ± 0.24
1256		D	0.05 ± 0.01	2.33 ± 0.22
1439		C or P	0.05 ± 0.01	1.17 ± 0.26
1578		D	0.06 ± 0.01	2.56 ± 0.20
1746		D	0.05 ± 0.01	2.72 ± 0.22
1748		D	0.05 ± 0.01	2.53 ± 0.21
1877		D	0.07 ± 0.01	1.74 ± 0.19
1911		C or P	0.04 ± 0.01	1.55 ± 0.20
1941		M	0.15 ± 0.03	1.65 ± 0.22
2067		D	0.05 ± 0.01	1.83 ± 0.22
2312		D	0.06 ± 0.01	2.05 ± 0.25
3254		D	0.07 ± 0.01	2.19 ± 0.22
3290	X	E	0.32 ± 0.08	1.90 ± 0.34
3843	X	M	0.11 ± 0.01	1.43 ± 0.21
4196		D	0.07 ± 0.01	2.02 ± 0.23
4317		D	0.05 ± 0.01	2.19 ± 0.18
5603		D	0.05 ± 0.01	1.97 ± 0.25
5928		D	0.05 ± 0.01	2.44 ± 0.25
6984		D	0.04 ± 0.01	2.60 ± 0.26
7027		D	0.07 ± 0.01	1.95 ± 0.19
7174		D	0.07 ± 0.01	1.59 ± 0.22
8550		C or P	0.05 ± 0.01	1.07 ± 0.23
8915		D	0.06 ± 0.01	2.40 ± 0.20
10331		M	0.13 ± 0.02	1.12 ± 0.19
11542	X	D	0.06 ± 0.01	1.78 ± 0.17
13035		C or P	0.05 ± 0.01	1.30 ± 0.22
15231		D	0.06 ± 0.01	1.98 ± 0.19
15376		D	0.08 ± 0.01	1.51 ± 0.24
15638		D	0.06 ± 0.01	2.00 ± 0.21
20038		D	0.08 ± 0.01	1.77 ± 0.19
31817		D	0.09 ± 0.01	1.68 ± 0.20
32460		M	0.10 ± 0.02	1.19 ± 0.23
38613		D	0.05 ± 0.01	3.19 ± 0.24
47907		D	0.07 ± 0.01	1.78 ± 0.23
61042		D	0.07 ± 0.01	1.97 ± 0.22

objects, due to their low slopes (i.e., low p_{IR}/p_V) and moderate visible albedos. Additional spectral observations are needed to confirm these classifications or possibly reclassify them as D-type asteroid as indicated by their location in Figure 12.

5.4. Hilda and Schubart Collisional Families

Brož & Vokrouhlický (2008) have identified two potential collisional families in the Hilda populations: one centered on (153) Hilda and the other on (1193) Schubart.

We observed 219 of the 360 members identified by Brož & Vokrouhlický (2008)⁹ and their weighted mean albedo is 0.061 ± 0.011 . The albedo distribution is shown in Figure 13 and is seen to be brighter than the full Hilda population. Our value is almost 50% brighter than the value used by Brož & Vokrouhlický (2008) and Brož et al. (2011) in attempts to derive the size of the parent body of this collisional family. Thirteen of the objects in this family have p_{IR}/p_V derived, and all except for two, (153) Hilda and (65374) 2002 PP55, are found to be in the D-type cluster in Figure 12. This is contrary to that stated in Brož et al. (2011), which claimed that most objects in the Hilda collisional family are C-type objects based on the spectral slopes derived from SDSS photometry (Ivezic et al. 2002; Parker et al. 2008; Gil-Hutton & Brunini 2008).

For the Schubart collisional family, we observed 112 out of the 232 objects identified by Brož & Vokrouhlický (2008) as members. The weighted mean of this family is 0.039 ± 0.013 and is clearly darker than that of the Hilda family (see Figure 13). Four of the objects observed had flux in either $W1$, $W2$, or both allowing the relative reflectance, p_{IR}/p_V . Following the discussion above on classification of objects, all four are found to be in the C- and P-type clusters in Figure 12.

5.5. The Size–Frequency Distribution

One of the important questions regarding the Hilda populations is its size and albedo distribution. Ryan &

⁹ Lists of members of the Hilda and Schubart collisional families were taken from the homepage of M. Brož at http://sirrah.troja.mff.cuni.cz/~mira/mp/trojans_hildas/.

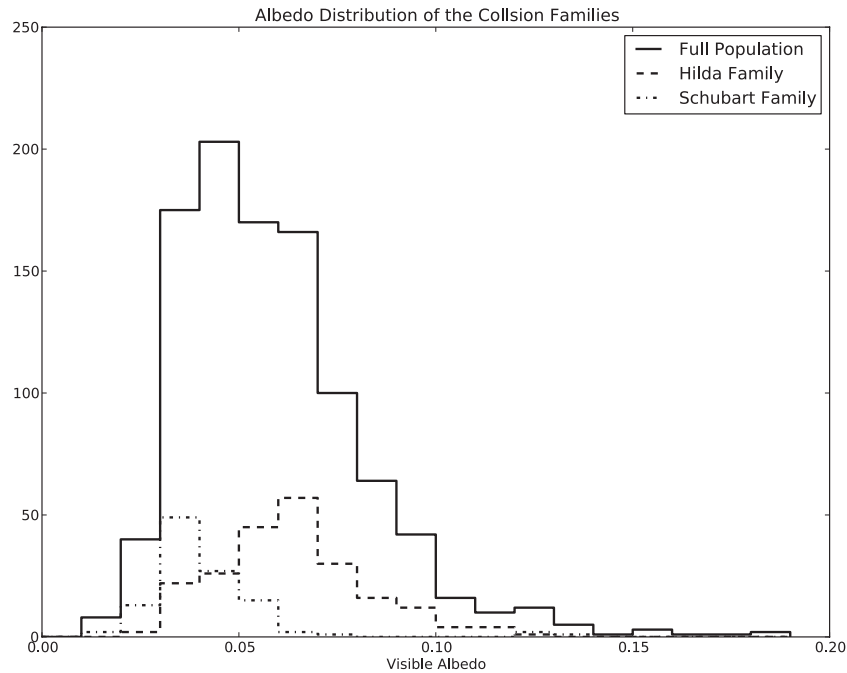


Figure 13. Visible albedo, p_V , of the two known collisional families identified by Brož & Vokrouhlický (2008) in the Hilda population.

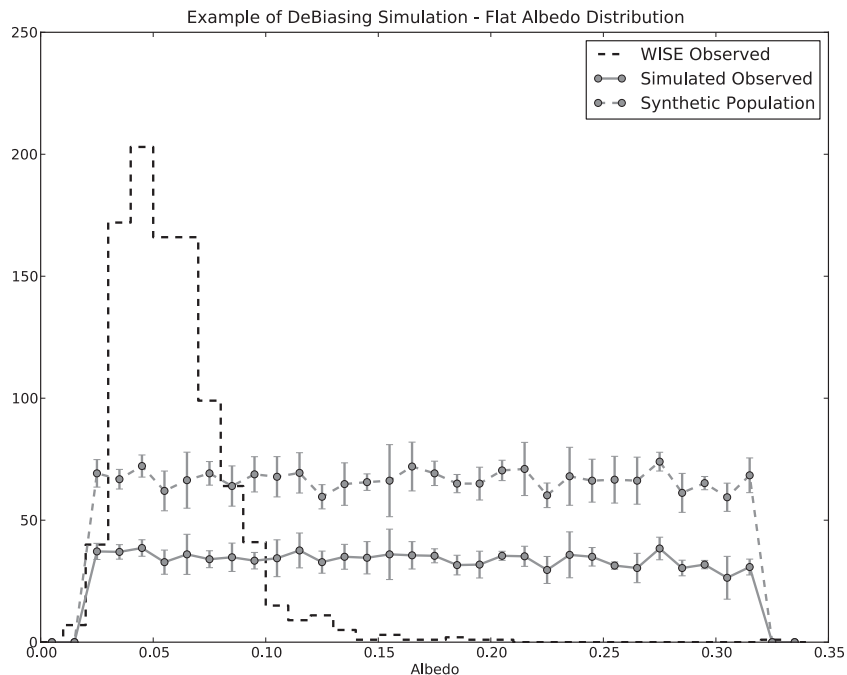


Figure 14. Visible albedo, p_V , distributions of the synthetic population and simulated observed sample using a flat albedo distribution are shown. The albedo bias is given by dividing the simulated distribution by the synthetic, which for the albedo yields essentially a flat bias. This means that the NEOWISE survey is equally sensitive to low and high albedos. The distribution of the albedos of the Hilda population as detected by NEOWISE is shown for comparison.

Woodward (2011) found a significant size–albedo correlation, where smaller objects have significant higher albedo than the larger objects. It is important to note that when they applied this size–albedo relation to the known sample to derive the size–frequency relationship, their results showed a very shallow slope for the objects in 5–12 km range. We believe that Ryan & Woodward (2011) incorrectly used the assumption that the optical surveys are currently complete to $V \sim 21.5$. Currently, optical surveys like the Catalina Sky Survey and Pan-STARRS (Wainscoat et al. 2010) routinely report new discoveries in the MBAs, Hildas, and Jovian Trojans that are

brighter than $V \sim 21.5$. Ryan & Woodward (2011) translated this assumption to a completeness for the Hilda population of $H \sim 15$. A quick look at the MPC orbital database reveals that there are ~ 1389 known objects in the Hilda population with $H < 15$, and 50 of these, making up $\sim 4\%$ – 5% of the known sample with $H < 15$, were discovered in the last two years. This shows that there most certainly is a low, but non-negligible, fraction of objects with $H < 15$ among the Hilda population that have yet to be discovered.

This problem is minor compared to the assumption that there is an albedo–size dependency, with the albedo increasing

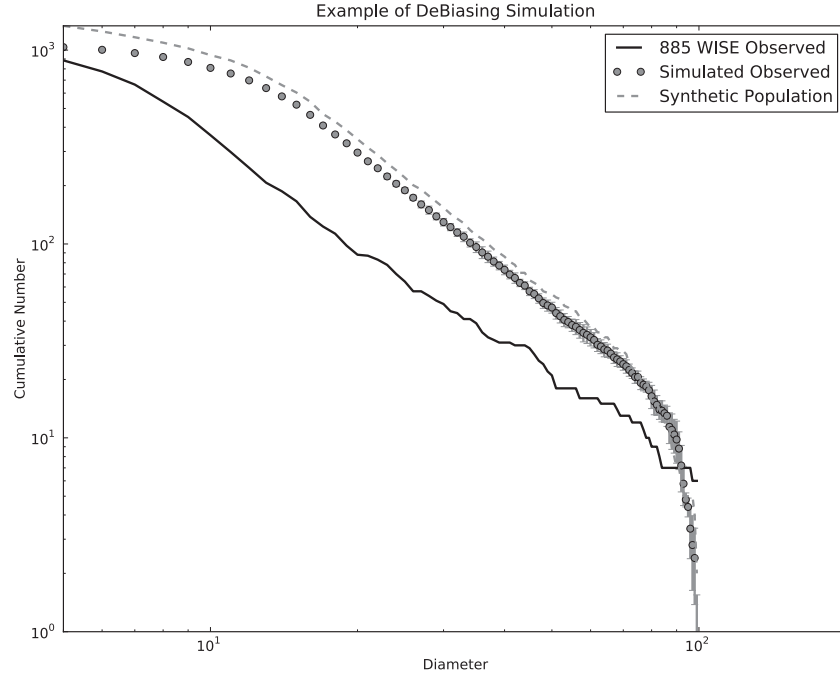


Figure 15. Size distribution of the synthetic population based on the albedo, size–frequency, and number distributions reported in Ryan & Woodward (2011) is shown as a dashed line (using 1334 objects larger than 5 km). The resulting simulated observations, the mean and standard deviation based on five simulations, are shown as gray points with associated error bars. The size–frequency of the 885 objects with $D > 5$ km observed by *WISE* is shown as a solid line. The resulting simulated distribution is clearly not consistent with the sample detected with NEOWISE.

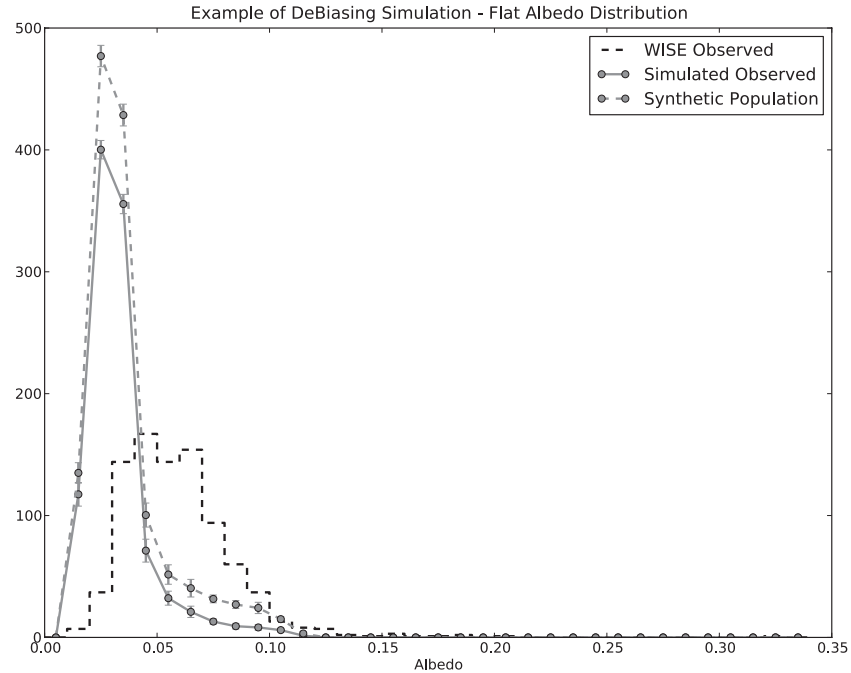


Figure 16. Visible albedo, p_V , distributions of the synthetic population and simulated observed sample based on Ryan & Woodward (2011) are shown in gray. The resulting simulated distribution is clearly not consistent with the sample detected with NEOWISE (here shown in black).

significantly for smaller sizes, which does not seem to be supported by our results. It could, however, be that our survey is simply significantly less sensitive to the higher albedo objects. In order to test this we have developed a survey simulator that mimics the real survey performed by NEOWISE and it is briefly described in Grav et al. (2011b) and discussed in detail in Mainzer et al. (2011b). A synthetic population of the Hildas was generated based on Grav et al. (2011a), assuring that the main feature of the orbital distribution was retained. The most

complex feature to duplicate is the triangular shape formed by the Hilda population (with its corners at $\pm 60^\circ$ and 180° away from Jupiter in its orbit), but this was easily accomplished by remembering that the Hildas follow the librating critical argument $\sigma = 3\lambda_J - 2\lambda - \bar{\omega}$, where λ_J is the mean longitude of Jupiter, λ is the mean longitude of the asteroid, and $\bar{\omega}$ is the longitude of perihelion of the asteroid (Brož et al. 2011). For example, if the mean longitude with respect to Jupiter is $\pm 60^\circ$ or 180° , i.e., at the Jovian Trojan clouds or opposite the Sun from

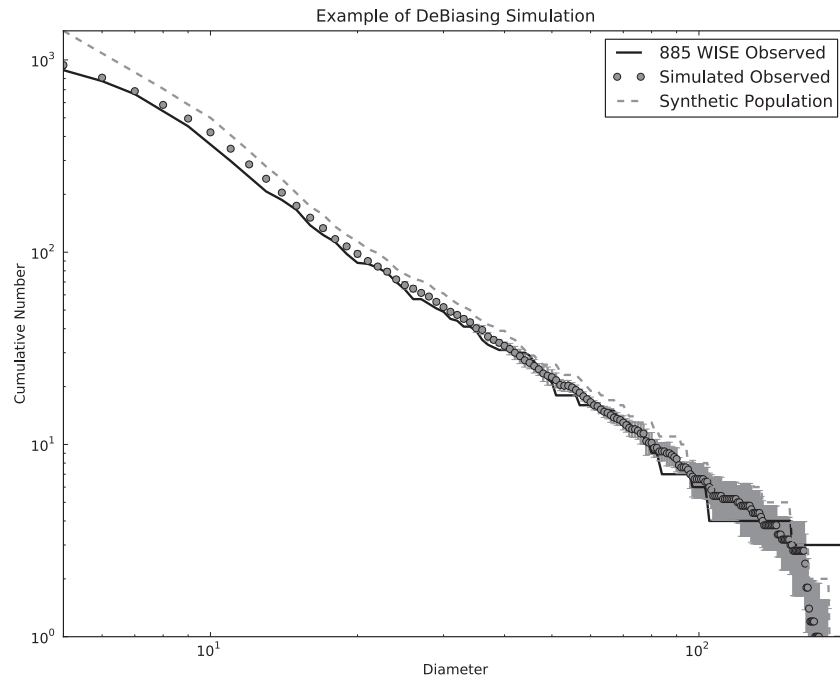


Figure 17. Size distribution of the synthetic population using a single-sloped power law with slope $\alpha = 1.7$ is shown as a dashed line. The resulting simulated observations, the mean and standard deviation based on five simulations, are shown as gray points with associated error bars. The size–frequency of the 885 objects with $D > 5$ km detected by NEOWISE is shown as a solid line. The resulting simulated distribution is nicely consistent with the sample detected with NEOWISE, although some refinement is clearly called for.

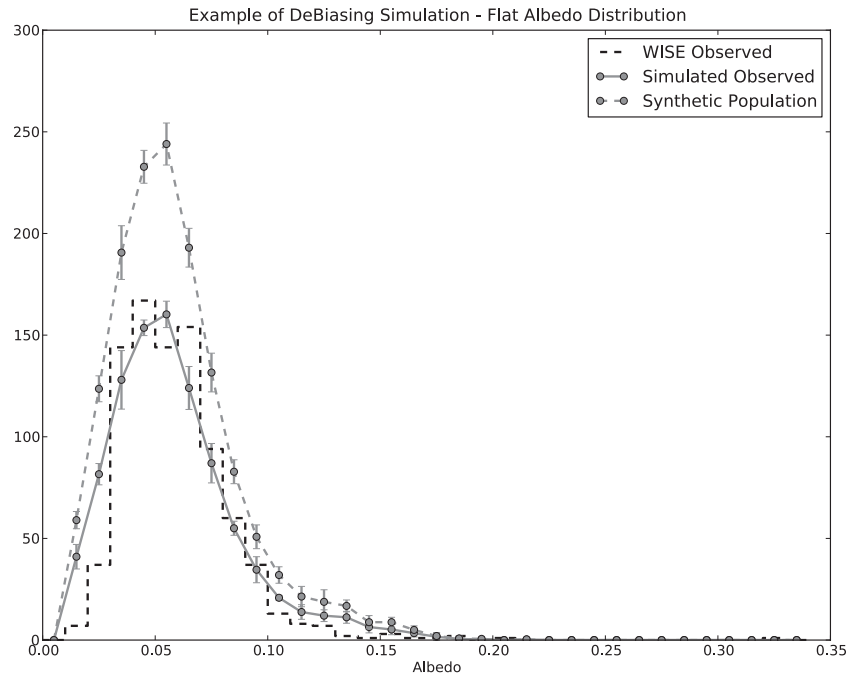


Figure 18. Visible albedo, p_V , distributions of the synthetic population using a single Gaussian with mean and standard deviation of 0.05 ± 0.03 are shown. The resulting simulated distribution is nicely consistent with the sample observed with *WISE*, although some refinement is clearly called for.

Jupiter, the object has to be at aphelion in its orbit, $M \sim 180^\circ$. Objects that are halfway in mean longitude between these three corners are at the perihelion point of their orbits, $M \sim 0^\circ$.

First we examine the bias that exists in the survey with respect to albedo. We use our Hilda synthetic population and assign each object a set of physical parameters. To test the albedo bias we use a random distribution of albedo ranging from 2% to 32% for each object; the beaming was given as a Gaussian distribution with mean and standard deviation of 0.85 ± 0.12 . We tested both

the size–frequency distribution given by Ryan & Woodward (2011) as well as a single power law of $N(>D) \sim D^{-\alpha}$ with slope of $\alpha = 2.0$. The result was the same in all simulations, showing no significant bias for all values of albedo (see Figure 14). This strengthens our concern that the size–albedo distribution reported by Ryan & Woodward (2011) is erroneous and a result of an observational bias caused by selecting the *Spitzer* targets from objects discovered solely by visible light surveys, which preferentially select

against small, low-albedo objects. Note that our sample from NEOWISE does not suffer from such selection biases as it is essentially a *blind* survey, using no a priori information in searching the data sets for both known and new minor planets.

We then moved on to testing the albedo distribution and size–frequency derived by Ryan & Woodward (2011). If their result is correct, we should be able to generate a synthetic population following these distributions, run this synthetic population through our survey simulator, and recover a simulated observed set of objects that is nearly identical to our sample of Hildas detected by NEOWISE. The results of our simulations are shown in Figures 15 and 16. Note that the albedo distribution of Ryan & Woodward (2011) was broadened slightly by varying the albedo of each object derived from their albedo–diameter relation by a random shift between $\pm 2\%$ to account for a more realistic error estimate. The resulting simulated distributions are clearly not consistent with the sample detected by NEOWISE.

A full debiasing of the Hilda population is beyond the scope of this paper; however, we have compared the sample observed by *WISE* with a handful of single-sloped power laws for the size–frequency distribution and single Gaussians for the albedo distributions. An example of the resulting simulations is shown in Figures 17 and 18. The single-sloped power law with a slope of $\alpha = 1.7 \pm 0.3$ is a much better fit than the distribution given by Ryan & Woodward (2011) and no significant break at $D \sim 12$ km is seen. Additional work is needed to derive refined estimates of the size–frequency and albedo distributions, and this work is underway. Future work also includes comparison of the numbers, sizes, and albedo distributions of the Hildas that we have computed to theoretical predictions based on various formation and evolution scenarios. It is, however, clear from this paper that the conclusions drawn in Ryan & Woodward (2011) are unsupported in our data set, which consists of more than one order of magnitude additional objects in the Hilda population with thermal modeling.

6. CONCLUSIONS

We derived thermal models for 1023 objects in the Hilda population, with sizes ranging from 3 to 200 km, that were observed during the cryogenic part of the NEOWISE survey. The Hildas are found to have a low albedo, weighted mean of 0.055 ± 0.018 , with most of the objects being consistent with having a C-, P- and D-type taxonomic classifications. Although there is an apparent broadening of the population at smaller sizes, this is found to be due to a natural increase in measurement outliers following Gaussian errors due to the increased number of objects at smaller sizes. For example, the weighted mean of the objects with diameter in the 4–5 km range is 0.049 ± 0.021 .

There are, however, a handful of objects with higher albedos and possible M- and E-type taxonomy that may be interlopers, coming from other parts of the solar system and subsequently captured in the 3:2 mean motion resonance. Furthermore, we find that the D-types dominate among the large Hildas (with $D > 30$ km), making up $67^{+7}_{-15}\%$. This is compared to $26^{+17}_{-5}\%$ of these objects being C-/P-type (with the majority of these being P-type asteroids).

We observed 219 and 112 of the members of the Hilda and Schubart collisional families, respectively. The results show that the Hilda collisional family is slightly brighter than the general population with a weighted mean albedo of 0.061 ± 0.011 , while the Schubart family is significantly darker with a weighted mean albedo of 0.039 ± 0.013 . Of the 220 objects observed in the

Hilda family, 13 have derived p_{IR}/p_V values that together with p_V indicate that all but two are D-type asteroids. We were only able to classify four of the Schubart family, with all of them falling in the C-/P-type clusters in Figure 12.

We also showed the size–frequency and size–albedo dependency found in Ryan & Woodward (2011) to be inconsistent with the results found by the NEOWISE survey. The albedos have no significant size–albedo dependency, and small objects have similarly dark surfaces as the larger objects. This result means that the size–frequency distribution derived by Ryan & Woodward (2011) is also in question. We compared their size–frequency distribution with that of a single-sloped power law with $\alpha \sim 1.7 \pm 0.3$ and found that the latter is a much better fit to the distribution detected by NEOWISE. This suggests that the Hildas are in near-collisional equilibrium (Dohnanyi 1969) for all sizes sampled in the NEOWISE survey. More work is needed, however, to more accurately debias our observed sample and derive the underlying, debiased size–frequency and albedo distributions.

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